

$$y = y_0 + v_{0y}t + \frac{1}{2}a_y t^2 = v_0 \sin(\Theta) t - \frac{1}{2}gt^2$$

$$x = x_0 + v_{0x}t + \frac{1}{2}a_x t^2 = v_0 \cos(\Theta) t$$

$$y = x \tan(\alpha)$$

$$t = \frac{x}{v_0 \cos(\Theta)}$$

$$x = \frac{RS}{\sqrt{1 + \tan^2(\alpha)}}$$

$$x \tan(\alpha) = v_0 \sin(\Theta) \frac{x}{v_0 \cos(\Theta)} - \frac{1}{2}g \left( \frac{x}{v_0 \cos(\Theta)} \right)^2$$

$$x \tan(\alpha) = x \tan(\Theta) - \frac{gx^2}{2v_0^2 \cos^2(\Theta)}$$

$$0 = x(\tan(\Theta) - \tan(\alpha)) - \frac{gx^2}{2v_0^2 \cos^2(\Theta)}$$

$$0 = x \left[ \tan(\Theta) - \tan(\alpha) - \frac{gx}{2v_0^2 \cos^2(\Theta)} \right]$$

$$\tan(\Theta) - \tan(\alpha) = \frac{gx}{2v_0^2 \cos^2(\Theta)}$$

$$x = \frac{2v_0^2 \cos^2(\Theta)(\tan(\Theta) - \tan(\alpha))}{g}$$

$$\frac{RS}{\sqrt{1 + \tan^2(\alpha)}} = \frac{2v_0^2 \cos^2(\Theta)(\tan(\Theta) - \tan(\alpha))}{g}$$

$$gRS = 2v_0^2 \cos^2(\Theta)[\tan(\Theta) - \tan(\alpha)]\sqrt{1 + \tan^2(\alpha)}$$